



## Imaginary Cycles of Permutations for Genus $g=3$ in Complex Geometries

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Imaginary cycles of permutations for *genus*  $g = 3$  in complex geometries

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**Abstract**

Considering a semi-state configurations taking genus  $g = 3$  for any complex geometries generalized over  $(+1)$  and  $(-1)$  structures with the fibers  $\mathcal{F}^\times \ni \times = \infty \forall \mathcal{F} \cong \oplus^k$  where  $k = \coprod_{\ell=\infty} (g_1^{\mathcal{F}^\times}, g_2^{\mathcal{F}^\times}, g_3^{\mathcal{F}^\times})^\ell / \sim$  defined through classes  $[\mathcal{O}_0]$ . Imaginary cycles being observed in *middle genus* for both left and right chirality over the vibrations of *unidirectional-cycles* enumerating over those fibers.

**Key words:** Complex structures; string theory.

**Mathematical subject classification:** 14-XX, 57-XX, 83Exx

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## Methods

Analyzing the vibrations of a single string is difficult to account for in course of making this paper, thus a bundled strings considering as a *fiber* is depicted throughout this work. Configurations set up is of three geometric curvatures, viz. Euclidean for  $\Omega = 0$ , elliptic for  $\Omega = +1$ , hyperbolic for  $\Omega = -1$ . A state being considered for  $\Omega = +1, -1$  topologies as is common in every hypercomplex and hyperbolic complex structures which in due proceedings in this paper – where a genus  $g = 3$  being incorporated in Ring  $\oplus^k$  being configured through fibers  $\mathcal{F}^\times$  as,

$$\mathcal{F}^\times \exists \times = \infty, \forall \mathcal{F} \cong \oplus^k \text{ where } k = \prod_{\ell=\infty} (g_1^{\mathcal{F}^\times}, g_2^{\mathcal{F}^\times}, g_3^{\mathcal{F}^\times})^\ell / \sim$$

Here  $\ell$  is being taken over towards infinity with each  $k$  being closed through equivalence after the disjoint union occurring through the each states being analyzed here. Considering the topologies as  $\sigma_{C-Y}$  being generalized over  $\Omega = +1, -1$  a circuit and a reverse circuit is established via  $\Sigma_0$  passing from  $d_1$  to  $d_2$  and reverse as,

$$\begin{aligned} \Sigma_{0 \cong +1} &\xrightarrow{d_1} \Sigma_{0 \cong 0} \xrightarrow{d_2} \Sigma_{0 \cong -1} \quad \forall +1 \rightarrow -1 \\ \Sigma_{0 \cong -1} &\xleftarrow{d_2} \Sigma_{0 \cong 0} \xleftarrow{d_1} \Sigma_{0 \cong +1} \quad \forall -1 \rightarrow +1 \end{aligned}$$

The groups are set up that being eventually help in establishing the cyclic permutations through the aforesaid genus as,

$\Psi^{-1}$	$\overline{\Psi+1\Psi^{-1}}$	$\Psi+1$
$\Sigma_{0 \cong -1}$	$\Sigma_{0 \cong 0}$	$\Sigma_{0 \cong +1}$
$\Omega = -1$	$\sigma_{C-Y}$	$\Omega = +1$

The chirality over those structures considering those vibrations could be analyzed taking the fibers passing through the  $g = 3$  genus configurations as,

<i>Left – Starting</i>	<i>Middle – Starting</i>	<i>Right – Starting</i>
$\partial$	$\partial \bar{\partial} - \partial \bar{\partial}^{-1}$	$\bar{\partial}$
<i>Permutation cycles</i>	<i>Defective Permutation cycles</i>	<i>Permutation cycles</i>

Denoting each element as matrix over permutation cycles as,

$$\partial = \begin{pmatrix} 1 & 2 & 3 & \cdots & n \\ 2 & 3 & 1 & \cdots & n \end{pmatrix}_{\forall g=3 \text{ iterations}}$$

$$\bar{\partial} = \begin{pmatrix} 3 & 2 & 1 & \cdots & n \\ 2 & 1 & 3 & \cdots & n \end{pmatrix}_{\forall g=3 \text{ iterations}}$$

$$\partial \bar{\partial} = \begin{pmatrix} 2 & 1 & \cdots & n \\ 1 & 2 & \cdots & n \end{pmatrix}_{\forall g=3 \text{ iterations}}$$

$$\partial \bar{\partial}^{-1} = \begin{pmatrix} 2 & 3 & \cdots & n \\ 3 & 2 & \cdots & n \end{pmatrix}_{\forall g=3 \text{ iterations}}$$

Thus, the imaginary cycles of permutations could be established via,

$$\partial \bar{\partial} - \partial \bar{\partial}^{-1} \equiv \left[ \begin{pmatrix} 2 & 1 & \cdots & n \\ 1 & 2 & \cdots & n \end{pmatrix} \cap \begin{pmatrix} 2 & 3 & \cdots & n \\ 3 & 2 & \cdots & n \end{pmatrix} \right]_{\forall g=3 \text{ iterations}}$$

Considering the 2<sup>nd</sup> genus being incapable to go over a complete cycles, the best that could be said is their permutation is indeed imaginary.

Generalizing this permutation cycles for all  $g = 3$  on all geometries normed through the fibers taking up the Rings for complex structures incorporated through,

$$\oplus^k \rightarrow \left( \begin{array}{c} \partial \\ \bar{\partial} \\ \partial \bar{\partial} - \partial \bar{\partial}^{-1} \end{array} \right)_{\forall g=3 \text{ iterations}} \quad \text{over all} \quad \left[ \begin{array}{c|c} \Psi^{-1} & \Sigma_{0 \cong -1} \\ \hline \overline{\Psi^{+1} \Psi^{-1}} & \Sigma_{0 \cong 0} \\ \Psi^{+1} & \Sigma_{0 \cong +1} \end{array} \right]$$

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